Hunslet Moor Primary School



Calculation Policy

Reviewed July 2024

Due to be reviewed July 2025

Addition Language

Year 1	+, add, more, plus, make, sum, total, altogether, score, double, near double, one more, two more ten more. How many more to make? How many more is than? How much more is? =, equals, sign, is the same as
Year 2	+, add, more, plus, make, sum, total, altogether, tens, ones, double, near double, one more, two more ten more. How many more to make? How many more is than? How much more is? =, equals, sign, is the same as
Year 3	+, add, addition, more, plus, make, sum, total, altogether, double, near double, one more, two more ten more one hundred more, How many more to make?, How many more is? Hundreds, Tens, Ones
Year 4	Add, addition, more, plus, increase, sum, total, altogether, double, near double How many more to make? Equals, sign, is the same as, tens boundary, hundreds boundary Inverse, Thousands, Hundreds, Tens, Ones
Year 5 & 6	Add, addition, more, plus, increase, sum, total, altogether, double, near double How many more to make? Equals, sign, is the same as, tens boundary, hundreds boundary Inverse, Millions, Thousands, Hundreds, Tens, Ones

Objective & Strategy	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part- whole model	Use part part whole model. Use cubes to add two numbers together as a group or in a bar.	Use pictures to add two numbers together as a group or in a bar.	4 + 3 = 7 Use the part-part whole diagram as shown above to move into the abstract.
Starting at the big- ger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	12 + 5 = 17 Start at the larger number on the number line and count on in ones or in one jump to find the answer.	5 + 12 = 17 Place the larger number in your head and count on the smaller number to find your answer.
Regrouping to make 10. This is an essential skill for column addition later.	Start with the bigger number and use the smaller number to make 10. Use ten frames.	3 + 9 = Use pictures or a number line. Regroup or partition the smaller number using the part part whole model to make 10. $9 + 5 = 14$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $2 + 4$ $3 + 6$ $3 + 6$ $4 + 6$ $4 + 6$ $5 + 6$ $5 + 6$ 6 6 $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ $1 + 6$ 1	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?
Represent & use number bonds and related subtraction facts within 20	2 more than 5.	012345878910 012345878910 0104/2 more hala	Emphasis should be on the language '1 more than 5 is equal to 6.' '2 more than 5 is 7.' '8 is 3 more than 5.'

Objective &	Concrete	Pictorial	Abstract
Strategy			
Adding multiples of	50= 30 = 20		20 + 30 = 50
ten	11111		70 = 50 + 20
		3 tens + 5 tens = tens 30 + 50 =	40 + □ = 60
	Model using dienes and bead strings	Use representations for base ten.	
Use known number facts Part part whole	Children explore ways of making numbers within 20	20 — — — — — — — — — — — — — — — — — — —	1 + 1 = 16
	N. C.	+= 20 20=	
Using known facts	+ =	□ + + + = .4.	3 + 4 = 7
	חחח חחח חחחחחח	1(1 + 111) = 11((1)	leads to
			30 + 40 = 70
		• • • • • • • • • • • • • • • • • • • •	leads to
		Children draw representations of H,T and O	300 + 400 = 700
Bar model		<u> </u>	23 25
		3333333 3 3 3	23 25
	3 + 4 = 7		
	J . 4 = 1	7 + 3 = 10	23 + 25 = 48

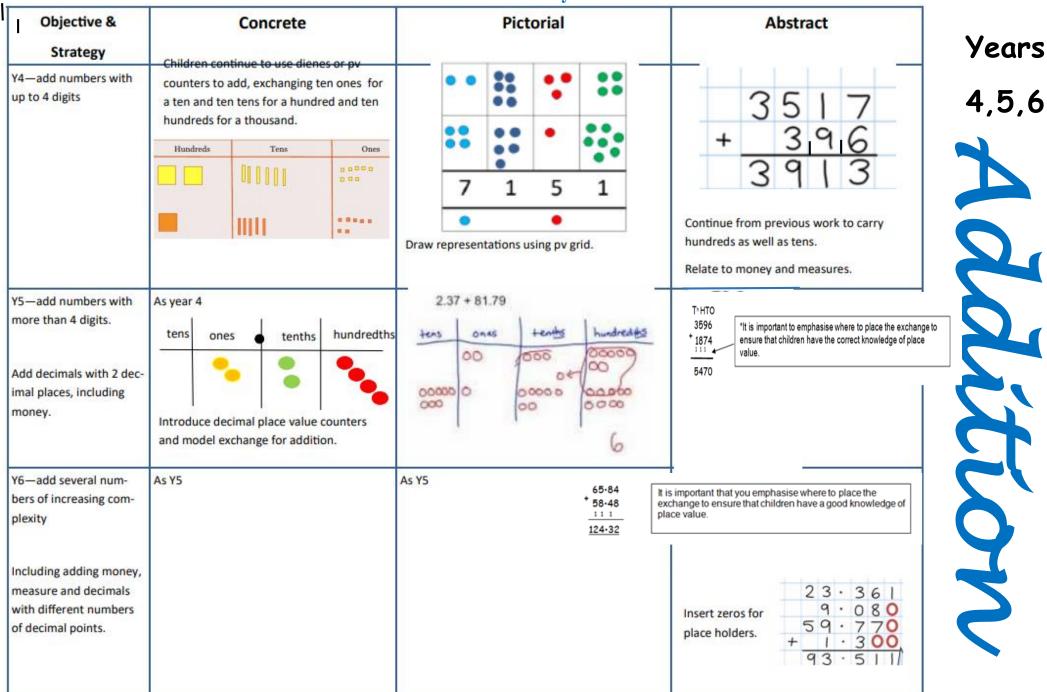
Objective &	Concrete	Pictorial	Abstract
Strategy			
Add a two digit number and ones	Use ten frame to make 'magic ten Children explore the pattern. 17 + 5 = 22 27 + 5 = 32	Use part part whole and number line to model. 17 + 5 = 22 3 2 16 + 7 16 20 23	17 + 5 = 22 Explore related facts 17 + 5 = 22 5 + 17 = 22 22
Add a 2 digit num- ber and tens	25 + 10 = 35 Explore that the ones digit does not change	27 + 30 +10 +10 +10 	27 + 10 = 37 27 + 20 = 47 27 + \(\sigma\) = 57
Add two 2-digit numbers	Model using dienes , place value counters and numicon	+20 +5 Or +20 +3 +2 47 67 72 47 67 70 72 Use number line and bridge ten using part whole if necessary.	25 + 47 $20 + 5$ $40 + 7$ $20 + 40 = 60$ $5 + 7 = 12$ $60 + 12 = 72$
Add three 1-digit numbers	Combine to make 10 first if possible, or bridge 10 then add third digit	Regroup and draw representation. + = 15	4+7+6 = 10+7 = 17 Combine the two numbers that make/ bridge ten then add on the third.

Year



Objective &	Concrete	Pictorial	Abstract
Strategy			
Column Addition—no regrouping (friendly numbers)	T O Model using Dienes or numicon Add together the ones first, then the	Children move to drawing the counters using a tens and one frame.	2 2 3
Add two or three 2 or 3-digit numbers.	tens. Tens Units 45 34 7 9 Cakulations 21+42= 21 42 Move to using place value counters	tens ones	+ 1 1 4 3 3 7 Add the ones first, then the tens, then the hundreds.
Column Addition with regrouping.	Tens Units 39 15 5 4 Exchange ten ones for a ten. Model using numicon and pv counters. Cakudatiers 146 + 527	Children can draw a representation of the grid to further support their understanding, carrying the ten underneath the line	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$





Subtraction Language

Year 1	-, subtract, take (away), minus, how many are left/left over? How many have gone? One less, two less, ten lesshow many fewer is than? How much less is? Difference between, half, halve =, equals, sign, is the same as, is of equal value to.
Year 2	Subtract, subtraction, take (away), minus, How many are left/left over? One less, two less ten less one hundred less, how many fewer is than? How much less is? Difference between, half, halve, equals, sign, is the same as, exchange, trade, ones, tens.
Year 3	Subtract, subtraction, take (away), minus, how many are left/left over? One less, two less ten less one hundred less, how many fewer is than? How much less is? Difference between, half, halve, equals, sign, is the same as, exchange, trade, hundreds, ones, tens.
Year 4, 5 & 6	Subtract, subtraction, take (away), minus, decrease, inverse, how many are left/left over? One less, two less ten less one hundred less, how many fewer is than? How much less is? Difference between, half, halve, equals, sign, is the same as, exchange, trade, thousands, hundreds, ones, tens, decimal.



Objective & Strategy	Concrete	Pictorial	Abstract
Taking away ones.	Use physical objects, counters, cubes etc to show how objects can be taken away. 6—4 = 2		7—4 = 3
	4-2=2	$15 - 3 = \boxed{12}$ Cross out drawn objects to show what has been taken away.	16—9 = 7
Counting back	Move objects away from the group, counting backwards. Move the beads along the bead string as you count backwards.	5 - 3 = 2 Count back in ones using a number line.	Put 13 in your head, count back 4. What number are you at?
Find the Difference	Compare objects and amounts 7 'Seven is 3 more than four' 4 'I am 2 years older than my sister'	Count on using a number line to find the difference. +6	Hannah has 12 sweets and her sister has 5. How many more does Hannah have than her sister.?

3 Erasers ? Lay objects to represent bar model.

Objective &	Concrete	Pictorial	Abstract
Strategy Represent and use number bonds and related subtraction facts within 20 Part Part Whole model	Link to addition. Use PPW model to model the inverse. If 10 is the whole and 6 is one of the arts, what s the other part? 10—6 = 4	Use pictorial representations to show the part.	Move to using numbers within the part whole model. 5
Make 10	Make 14 on the ten frame. Take 4 away to make ten, then take one more away so that you have taken 5.	13—7 13—7=6 3 4 3 4 3 4 3 4 3 4 3 4 3 4 4 5 3 4 5 5 6 5 6 7 5 7 5 7 5 7 5 7 5 7	16—8 How many do we take off first to get to 10? How many left to take off?
Bar model	5-2 = 3	**************************************	8 2 10 = 8 + 2

10 = 2 + 8

10-2 = 8

10-8 = 2

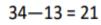
Year
2



		•	
Objective & Strategy	Concrete	Pictorial	Abstract
Regroup a ten into ten ones	Use a PV chart to show how to change a ten into ten ones, use the term 'take and make'	20 – 4 =	20—4 = 16
Partitioning to sub-	24 12 21 999	Children draw representations of Dienes and	

Partitioning to subtract without regrouping.

'Friendly numbers'





Use Dienes to show how to partition the number when subtracting without regrouping.



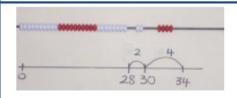


cross off.



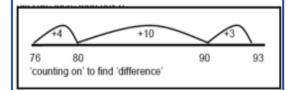
Make ten strategy

Progression should be crossing one ten, crossing more than one ten, crossing the hundreds.



counting to next ten and the rest.

34 - 28Use a bead bar or bead strings to model



Use a number line to count on to next ten and then the rest.

$$93 - 76 = 17$$



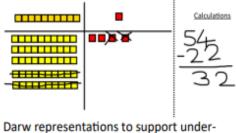


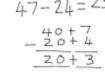
Objective & Strategy	Concrete	Pictorial	Abstract
Column subtraction without regrouping (friendly numbers)	47—32	Calculations 5/4 -2/2	47-24=23 _ 2 0+7

standing



Use base 10 or Numicon to model





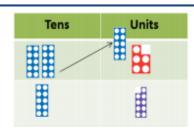
Intermediate step may be needed to lead to clear subtraction understanding.

Begin by parti-

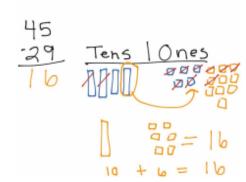
tioning into pv

columns

Column subtraction with regrouping



Begin with base 10 or Numicon. Move to pv counters, modelling the exchange of a ten into tten ones. Use the phrase 'take and make' for exchange.



Children may draw base ten or PV counters and cross off.

728-582=146

Then move to formal method.

Objective &	Concrete	Pictorial	Abstract
Strategy			
Subtracting tens and ones Year 4 subtract with up to 4 digits. Introduce decimal subtraction through context of money	234 - 179	Children to draw pv counters and show their exchange—see Y3	2 X 5 4 - 1 5 6 2 1 1 9 2 Use the phrase 'take and make' for exchange
Year 5- Subtract with at least 4 dig- its, including money and measures. Subtract with decimal values, including mixtures of integers and decimals and aligning the decimal	As Year 4	Children to draw pv counters and show their exchange—see Y3 Th HT O 15 0 4 - 2 7 5 Where do we record this?	*3 * X '0 * 8 '6 - 2 2 8 2 8 9 2 8 Use zeros for place-holders. - 3 7 2 5 5 5 6 7 9 6 5 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 5 6 7 9 6 5 6 7 9 6 5 6 7 9 6 5 7 9 6 5 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 6 7 9 9 9 9 9 9 9 9 9
Year 6—Subtract with increasingly large and more complex numbers and decimal values.			" " 8 10, 6 9 9 - 8 9, 9 4 9 6 0, 7 5 0 " 10 '5 · 3 4 '1 9 kg - 3 6 · 0 8 0 kg 6 9 · 3 3 9 kg

Years

4,5,6



Multiplication Language

Year 1	double, groups of, near double, equals, sign, is the same as
Year 2	lots of, groups of, x times, multiply, multiplied by, multiple of, once, twice, three times ten times, times as (big, long, wide and so on), repeated addition, array, row, column, double.
Year 3	lots of, groups of, x, times, multiply, multiplication, multiplied by, multiple of, product, once, twice, three times, times as (big, long, wide and so on), repeated addition, array, row, column, double,
Year 4 & 5	lots of, groups of, times, multiply, multiplication, multiplied by, multiple of, product, once, twice, three times, times as (big, long, wide and so on), repeated addition, array, row, column, double, factor, quotient, divisible by, inverse
Year 6	Halve, share, share equally, one each, two each, three each, group in pairs, threes tens, equal groups of, divide, division, divided by, divided into, remainder, factor, quotient, divisible by, inverse

Objective & Strategy	Concrete	Pictorial	Abstract
Doubling	Use practical activities using manipultives including cubes and Numicon to demonstrate doubling	Double 4 is 8	Partition a number and then double each part before recombining it back together. 16 10 6 1x2 1x2 20 + 12 = 32
Counting in multi- ples	Count the groups as children are skip counting, children may use their fingers as they are skip counting.	Children make representations to show counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30
Making equal groups and counting the total	□ x = 8 Use manipulatives to create equal groups.	Draw to show 2 x 3 = 6 Draw and make representations	2 x 4 = 8

Year

Objective & Strategy	Concrete	Pictorial	Abstract
Repeated addition	Use different objects to add equal groups	Use pictorial including number lines to solve prob There are 3 sweets in one bag. How many sweets are in 5 bags altogether? 3+3+3+3+3 = 15	Write addition sentences to describe objects and pictures. 2+2+2+2 = 10
Understanding ar- rays	Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.	Draw representations of arrays to show under- standing	3 x 2 = 6 2 x 5 = 10

Objective & Strategy	Concrete	Pictorial	Abstract
Doubling	Model doubling using dienes and PV counters. 40 + 12 = 52	Draw pictures and representations to show how to double numbers	Partition a number and then double each part before recombining it back together. 16 10 6 12 20 + 12 = 32
Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)	Count the groups as children are skip counting, children may use their fingers as they are skip counting. Use bar models. 5+5+5+5+5+5+5+5+5=40	Number lines, counting sticks and bar models should be used to show representation of counting in multiples. 3 3 3 3 3	Count in multiples of a number aloud. Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15 0, 5, 10, 15, 20, 25, 30

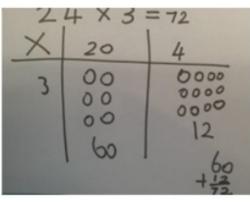
Objective & Strategy	Concrete	Pictorial	Abstract
Multiplication is commutative	Create arrays using counters and cubes and Numicon. Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.	Use representations of arrays to show different calculations and explore commutativity.	12 = 3 × 4 12 = 4 × 3 Use an array to write multiplication sentences and reinforce repeated addition. 5 + 5 + 5 = 15 3 + 3 + 3 + 3 + 3 = 15 5 x 3 = 15 3 x 5 = 15
Using the Inverse This should be taught alongside division, so pupils learn how they work alongside each other.		8	2 x 4 = 8 4 x 2 = 8 8 ÷ 2 = 4 8 ÷ 4 = 2 8 = 2 x 4 8 = 4 x 2 2 = 8 ÷ 4 4 = 8 ÷ 2 Show all 8 related fact family sentences.

Objective &	Concrete	
Strategy Grid method	Show the links with arrays to first intro-	С
	duce the grid method. x 10 3 4 rows of 10 4 rows of 3	Ti sh th
	Move onto base ten to move towards a	sl
	more compact method.	
	Move on to place value counters to show	Ш
	how we are finding groups of a number. We are multiplying by 4 so we need 4 rows	Ш
	© Calculations 4 x 126	
		В
	Fill each row with 126 Calculations 4 x 126	
	Add up each column, starting with the ones making any exchanges needed	
	Then you have your answer.	-

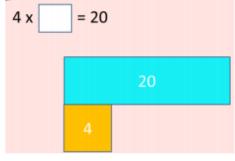
Children can represent their work with place value counters in a way that they understand.

Pictorial

They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.



Bar model are used to explore missing numbers



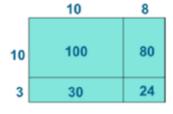
Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

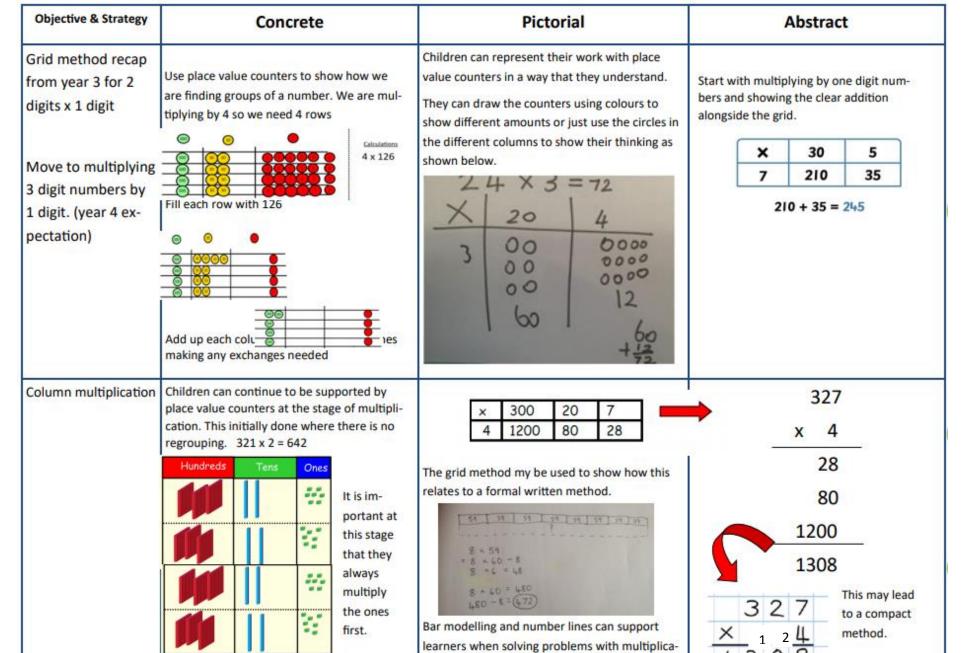
Abstract

×	30	5
7	210	35

$$210 + 35 = 245$$

Moving forward, multiply by a 2 digit number showing the different rows within the grid method.





tion alongside the formal written methods.

The corresponding long multiplication is mod-

elled alongside

Years 5&6

Maths Calculation Policy 2024-2025

Objective &	Concrete	Pictorial	Abstract
Strategy			
Column Multiplication for 3 and 4 digits x 1 digit.	Hundreds Tens Ones	× 300 20 7	327
	It is important at	4 1200 80 28	x _4
	this stage that they		28
	always		80
	the ones		1200
	first.		1308
	Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. 321 x 2 = 642		This will lead to a compact method.
Column multiplication	Manipulatives may still be used with the cor- responding long multiplication modelled alongside.	10 8 10 100 80 3 30 24	1 8 18 x 3 on the first row x 1 3 5 4 (8 x 3 = 24, carrying the 2 for 20, then 1 x 3) 2 3 4 18 x 10 on the
		Continue to use bar modelling to support prob- lem solving	2nd row. Show multiplying by 10 by putting 2ero in units first 19744

Objective &	Concrete	Pictorial	Abstract
Strategy			
Multiplying decimals up to 2 decimal places by a single digit.			Remind children that the single digit belongs in the units column. Line up the decimal points in the question and the answer. $\begin{array}{cccccccccccccccccccccccccccccccccccc$

Division Language

Year 1	Halve, share equally, one each, two each, three eachgroup in pairs, threes tens equal groups of, ÷, divide, divided by, divided into, left, left over, how many groups of
Year 2	Halve, share equally, one each, two each, three eachgroup in pairs, threes tens equal groups of, ÷, divided by, divided into, left, left over, how many groups of
Year 3	Halve, group, group equally, one each, two each, three each, group in pairs, threes tens, equal groups of, ÷ divide, division, divided by, divided into, left, left over, remainder
Year 4	Halve, group, group equally, one each, two each, three each, group in pairs, threes tens equal groups of, divide, division, divided by, divided into, remainder, factor, quotient, divisible by inverse
Year 5 & 6	Halve, group, group equally, one each, two each, three each, group in pairs, threes tens equal groups of, divide, division, divided by, divided into, remainder, short division, factor, quotient, divisible by, inverse

Objective & Strategy	Concrete	Pictorial	Abstract
Division as sharing Use Gordon ITPs for modelling		Children use pictures or shapes to share quantities. 8 Strateu Detween 2 is 4 Sharing: 12 shared between 3 is 4	12 shared between 3 is 4
	I have 10 cubes, can you share them equally in 2 groups?		



Objective & Strategy	Concrete	Pictorial	Abstract
Division as sharing	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. 8 + 2 = 4 Children use bar modelling to show and support understanding.	12 ÷ 3 = 4
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use number lines for grouping 12 ÷ 3 = 4 Think of the paras a whole, split it into the number of groups you are dividing by and work out how many would be within each group. 20 ÷ 5 = ? 5 x ? = 20	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?



Objective &	Concrete	Pictorial	Abstract
Strategy			
Division as grouping	Use cubes, counters, objects or place value counters to aid understanding. 24 divided into groups of $6 = 4$ 96 ÷ 3 = 32	Continue to use bar modelling to aid solving division problems. $ \begin{array}{c} 20 \\ ? \end{array} $ $ 20 \div 5 = ? $ $ 5 \times ? = 20 $	How many groups of 6 in 24? $24 \div 6 = 4$
Division with arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$	Draw an array and use lines to split the array into groups to make multiplication and division sentences	Find the inverse of multiplication and division sentences by creating eight linking number sentences. 7 x 4 = 28 4 x 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7 28 = 7 x 4 28 = 4 x 7 4 = 28 ÷ 7 7 = 28 ÷ 4



Objective & Strategy	Concrete	Pictorial	Abstract
Division with remainders.	Divide objects between groups and see how much is left over Example without 40 + 5 Ask "How many Example with re 38 + 6 For larger number jumps can be recommended."	5s in 40? 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 8 f	a remainder of 2

Year



Objective &	Concrete	Pictorial	Abstract
Divide at least 3 digit numbers by 1 digit. Short Division	96 ÷ 3 Tens Units 3 2 3 Use place value counters to divide using the bus stop method alongside Calculations 42 ÷ 3= Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.	Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups. Encourage them to move towards counting in multiples to divide more efficiently. 156 -7 - 2 7 × 10 70 × 10 140 × 2 154 × 2 156 × 156 - 7 - 22 - 156	Begin with divisions that divide equally with no remainder. 2 1 8 3 4 8 7 2 Move onto divisions with a remainder. 8 6 r 2 5 4 3 2 Finally move into decimal places to divide the total accurately. 1 4 6 16 21 3 5 5 1 1 . 0

Years

4,5,6



Long Division

Step 1—a remainder in the ones

- 4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).
- 4 goes into 16 four times.
- 4 goes into 5 once, leaving a remainder of 1.

- 8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200).
- 8 goes into 32 four times (3,200 + 8 = 400)
- 8 goes into 0 zero times (tens).
- 8 goes into 7 zero times, and leaves a remainder of 7.

Year Recognise, find and name a half as one of two equal parts of an object, shape or quantity. Concrete Pictorial Abstract A whole apple Half an apple Half of 10 = Half of 8 = of 14 = nise, Recog- $\frac{1}{2}$ find and name a quarter as one four equal parts of an object, shape or quantity. Concrete Abstract Pictorial A quarter of 20 = A quarter of 12 = of 8 =

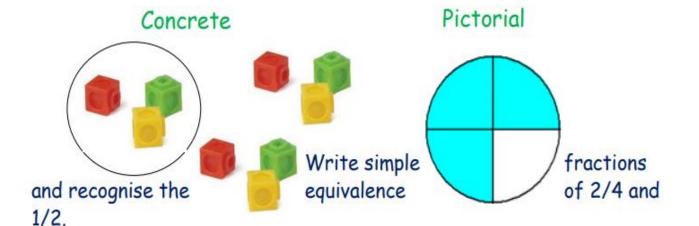
Year

2

Recognise, find and name and write fractions 1/3, 1/4, 2/4 and 3/4 of a length, shape, set of objects or quantity.

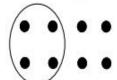
sear.





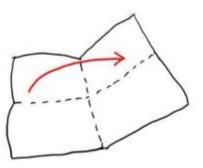


$$\frac{2}{4}$$
 of 8 =

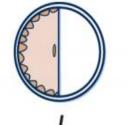




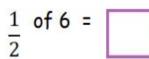
Concrete

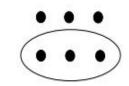


Pictorial



I have $\frac{1}{2}$ a pie You have $\frac{2}{4}$ of a pie





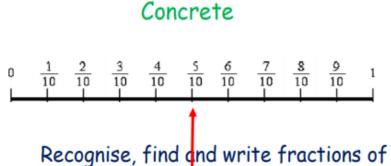


Count up and down in tenths: recognise that tenths arise from dividing an object into ten equal parts and in dividing one-digit numbers or quantities by ten.

Year

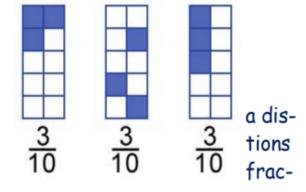
3

3



Recognise, find and write fractions of crete set of and non-unit $\frac{1}{2}$ fractions and use tions as numbers.

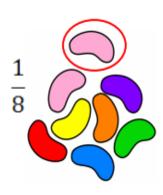
Pictorial



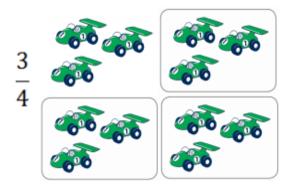
Abstract

$$\frac{1}{10}$$
 of 6 = 0.6
because
6 ÷ 10 = 0.6
 $\frac{1}{10}$ of 7 = 0.7
because
7 ÷ 10 = 0.7

Concrete



Pictorial



$$\frac{1}{5} \text{ of } 15 \text{ sweets} = 3$$

$$2 \text{ cause } 15 \div 5 = 3$$

$$\frac{2}{5}$$
 of 15 sweets = 6
beca $\frac{1}{5}$ 15 ÷ 5 = 3 and 3 x 2 = 6

Pictorial

Recognise and show, using diagrams, equivalent fractions with small denominators.

Year

Concrete

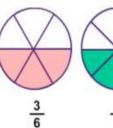


two halves

four quarters Add sub-







Abstract

Sam says that two quarters is the same as one half.

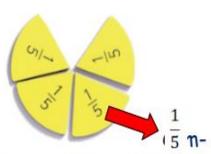
Is he correct?

How do you know?

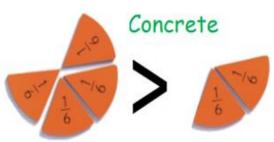
and

tract fractions with the same denominator.

Concrete



and order unit fractions the same denominators.



Pictorial



Pictorial



Abstract

$$\frac{5}{7} + \frac{1}{7} = \frac{6}{7}$$

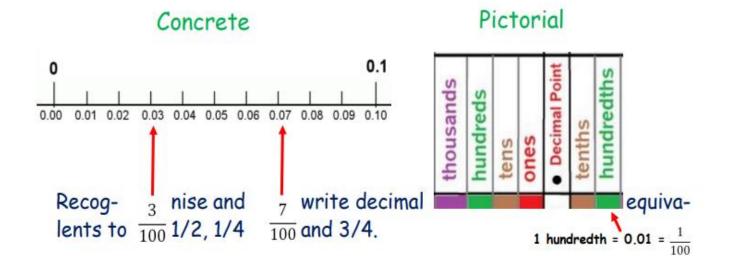
$$\frac{5}{8} - \frac{2}{8} = \frac{3}{8}$$
 pare with





Count up and down in hundredths: recognise that hundredths arise when dividing an object by 100 and dividing tenths by 10.

Year

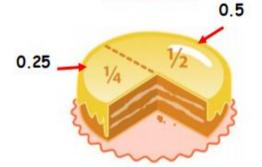


Abstract

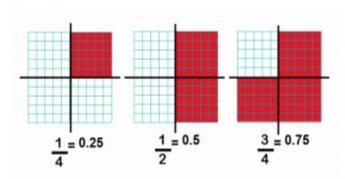
$$\frac{1}{100}$$
 of 60 = 0.6
because 60 ÷ 100 = 0.6

so
$$\frac{1}{100}$$
 of 70 = 0.7 of 70 = 0.07





Pictorial



$$\frac{1}{2} = 0.5$$

$$\frac{1}{4} = 0.25$$

$$\frac{1}{4} = 0.75$$

$$\frac{3}{4}$$

Concrete



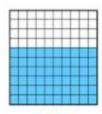
Rec- $\frac{1}{10}$ of the chocolate bar = 0.1

nator.

Pictorial



six tenths



0.60 sixty hundredths and show,

grams, families of common equivalents.

Abstract

$$\frac{1}{10}$$
 = 0.1

$$\frac{3}{10}$$
 = 0.3

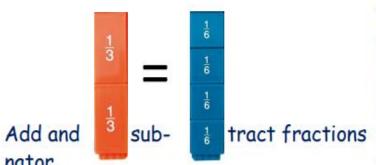
$$\frac{5}{10} = \frac{1}{2} = 0.5$$

$$\frac{8}{100} = 0.08$$
 using dia-

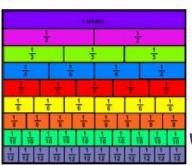
Year



Concrete



Pictorial



with the same

Abstract

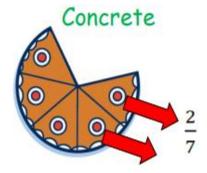
$$\frac{2}{3} = \frac{4}{6}$$

$$\frac{3}{5} = \frac{6}{10}$$

$$\frac{2}{12} = \frac{1}{6}$$

denomi-

Abstract







Pictorial

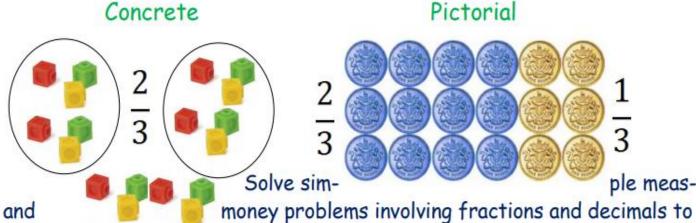


Sam eats 2 of a whole pizza. How much 7 oes he have left?

Lucy and Ben both eat of a cake. How much have they eat $\frac{3}{8}$ altogether?

Solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number.

Year



Pictorial Abstract

ple meas-

$$\frac{2}{3}$$
 of £18

£18 ÷
$$3 = £6$$

£6
$$\times$$
 2 = £12

ure

two

Concrete

decimal places.



Pictorial

U		t	h
Units	Decimal Point	Tenths	Hundredths
		A STATE OF THE STA	

$$50cm = \frac{1}{2} = 0.5m$$

$$25cm = \frac{1}{4} = 0.25m$$

$$10cm = \frac{1}{10} = 0.1m$$

$$30cm = \frac{3}{10} = 0.3m$$

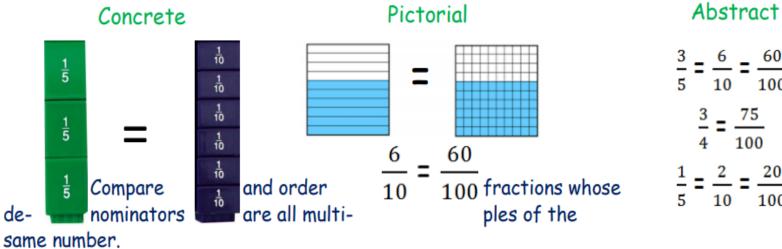


Identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths.

Year

5





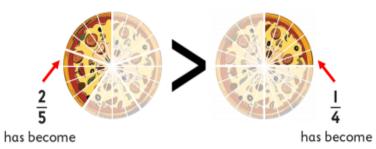
 $\frac{5}{20}$

$$\frac{3}{4} = \frac{73}{100}$$

$$\frac{1}{5} = \frac{2}{10} = \frac{20}{100}$$

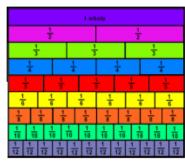


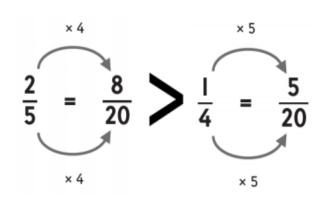




 $\frac{8}{20}$

Pictorial





Recognise mixed numbers and improper fractions. Convert from one form to the other and write mathematical statements >1 as a mixed number.

Year



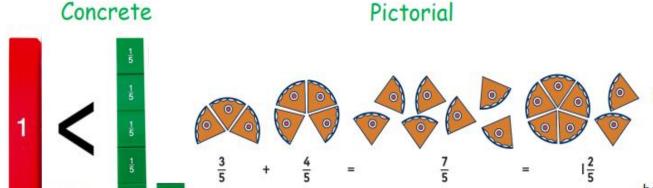


Abstract

$$\frac{7}{2} = 3\frac{1}{2}$$
because 7 ÷ 2 = 3 with 1 half left over

$$2\frac{1}{3} = \frac{7}{3}$$

because 2 x 3 = 6 with 1 third left to add



subtract fractions with the same denominators

and denominators that are multiples of the same numbers.

Abstract

$$\frac{2}{5} - \frac{1}{4}$$





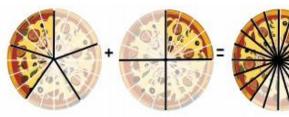
$\frac{8}{20}$	-	

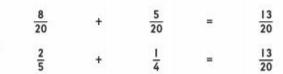
$$\frac{2}{5}$$



Add

and





Pictorial

Year

Multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams.

Concrete

Pictorial

Abstract

5















Multiply a proper fraction by a whole number

Change to a mixed number:

to

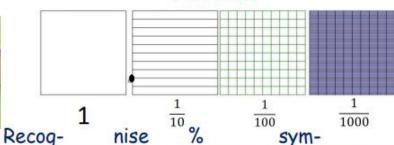
6 lots of $\frac{3}{4}$ tenths, hundredths and

Recognise and use $4\frac{2}{4}$ altogether thousandths and relate $\frac{18}{4} = 4\frac{2}{4}$ them decimal equivalents.

Concrete



Pictorial



Abstract

67.153

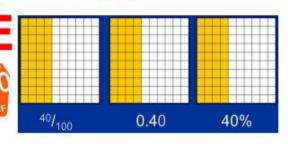
How many thousandths does this number have? How many more thousandths do you need to add to make 67.16?

bol and understand the meaning: write % as a fraction, decimal and percentage.

Concrete



Pictorial



$$\frac{4}{10}$$
 = 40% = 0.4

$$\frac{32}{100}$$
 = 32% = 0.32

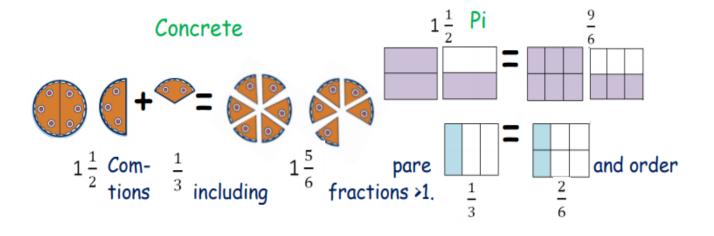
$$\frac{75}{100}$$
 = 75% = 0.75

$$\frac{2}{25} = \frac{8}{100} = 8\% = 0.08$$

Add and subtract fractions with different denominators and mixed numbers using the concept of equivalent fractions.

Year





Abstract

$$1\frac{1}{2} + \frac{1}{3} = 1\frac{5}{6}$$

because
$$1\frac{1}{2} = \frac{3}{2}$$

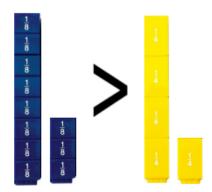
frac-

$$\frac{3}{2} = \frac{9}{6}$$
 and $\frac{1}{3} = \frac{2}{6}$

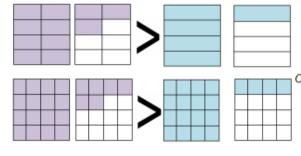
$$so^{\frac{9}{6}} + \frac{2}{6} = \frac{11}{6} = 1\frac{5}{6}$$



Concrete



Pictorial



Abstract

Which is greater?

$$\frac{2}{8} < \frac{6}{16}$$

Ordering from smallest to largest by using equivalent fractions:

$$\frac{5}{12}$$
, $\frac{2}{3}$, $\frac{5}{6}$

$$\frac{5}{12}$$
, $\frac{8}{12}$, $\frac{10}{12}$

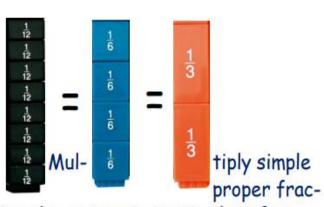
Use common factors to simplify fractions; use common multiples to express fractions in the same denomination.

Pictorial

Year

6

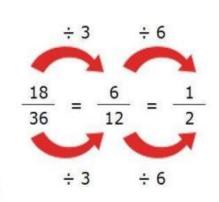
Abstract

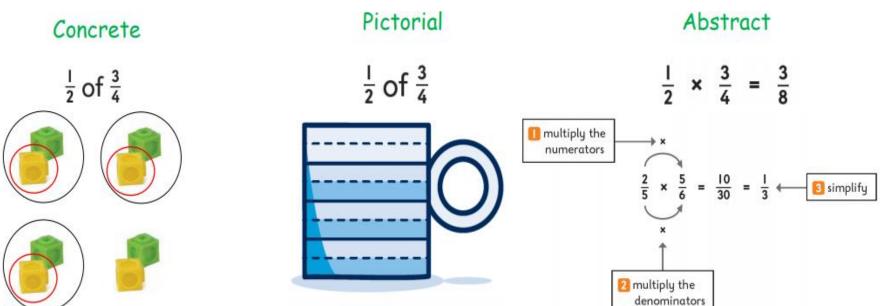


Concrete

ing the answer in its simplest form.









Recall and use equivalences between simple fractions, decimals and percentages including in different contexts.

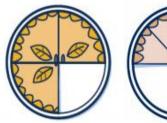
Year

Concrete



Pictorial

Which would you prefer 75% or $\frac{3}{8}$ of a pie?





 $\begin{array}{ccc}
 75\% & \frac{3}{8} \\
 \text{Divide} & \text{proper} & \frac{3}{8} \\
 \text{fractions} \\
 \text{by whole numbers.}
\end{array}$

Abstract

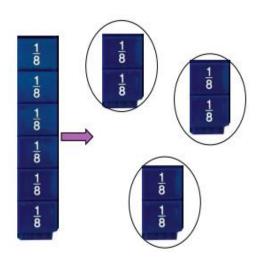
John scored $\frac{40}{80}$ in his spelling test and Hannah scored 40%. Who scored more?

One paving slab is 0.3m long and another
is of a metre. Which is longer?

1/4 = 0.25m

0.3m is larger than 0.25m

Concrete



Pictorial



$$\frac{1}{2} \div 3 = \frac{1}{6}$$

Abstract

$$\frac{1}{2} \div 3 = \frac{1}{6}$$

Keep it, change it, flip it!

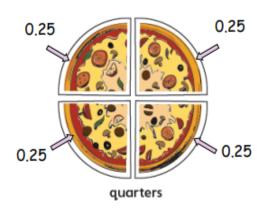
$$\frac{1}{2} \times \frac{1}{3} = \frac{1}{6}$$

Year

6

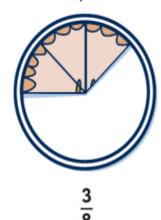
Associate fractions with division and calculate decimal fraction equivalents.

Concrete



Pictorial

3 slices of pie 'out of' 8



Abstract

<u>3</u>

3 'out of' 8 is the same as 3 'divided by' 8

$$3 \div 8 = 0.375$$

So
$$\frac{3}{8} = 0.375$$

